## **Department of Mathematics**

## **Course Profile**

Course Number : MATH 427	Course Title: Advanced Numerical Methods
Required / Elective : Elective	Prerequisite: None
<b>Catalog Description:</b> Numerical solution of ordinary differential equations, initial value and boundary value problems; an introduction to the numerical solution of elliptic, parabolic and hyperbolic partial differential equations.	Textbook / Required Material : "A First Course in the Numerical Analysis of Differential Equations", by A. Iserles, Published by Cambridge University Press, 2006. "Numerical Solution of Partial Diffrential Equations", by K. W. Morton and D. F. Mayers, Published by Cambridge University Press, 1994.
Course Structure / Schedule: (3+0+0) 3 / 7 ECTS	

## **Extended Description :**

The goal of this course is to study various numerical methods used for solving ordinary differential equations and partial differential equations. Most of the material to be covered can be found in chapters 1-4 of the first textbook and in chapters 2, 4-6 of the second textbook.

The first part of the course is about numerical solution techniques for ordinary differential equations (Euler's method, multis-tep methods, Runge-Kutta methods, stiff ordinary-differential equations). The second part of the course is devoted to finite-difference methods for parabolic, hyperbolic and elliptic partial differential equations (parabolic equations in one space dimension, hyperbolic equations in one space dimension, consistency, convergence and stability, linear second-order elliptic equations in two dimensions).

<b>Design content:</b> None.	Computer usage: No particular computer
	usage required.

Course Outcomes: [relevant program outcomes in brackets]:

By the end of the course the students should be able to:

- 1. state and understand the standard numerical methods for ordinary differential equations [2,3,5],
- 2. understand the concepts of the linear stability domain and A-stability [2,3,5]
- 3. derive finite-difference schemes for parabolic or hyperbolic differential equations [2,3,5]
- 4. understand the concepts of consistency, convergence and stability [2,3,5].

[2] demonstrate knowledge of mathematics to construct, analyze and interpret mathematical models,

[3] demonstrate the ability to apply mathematics to the solutions of problems,

[5] have an ability to write computer programs and use algorithms for solving problems,

<b>Recommended reading</b> : "Numerical Analysis: Mathematics of Scientific Computing" (Chapters 8,9), by D. Kincaid and W. Cheney, Published by Brooks/Cole, 2002.		
"Numerical Analysis" (Chapters 5, 10, 11), by R. L. Burden, J. D. Faires and A. C. Reynolds, Published by PWS Publishers, 1981.		
"Finite Difference Schemes and Partial Differential Equations" (Chapters 1-6, 8-10), by J. C. Strikwerda, Published by SIAM, 2004.		
Teaching methods: Preparatory-readings, lectures, discussions, assignments		
Assessment methods: Midterm exams, Final exam		
Student workload:		
Preparatory reading	54 hrs	
Lectures42 hrs		
Assignments56 hrs		
Discussions14 hrs		
Midterm exams6 hrs		
Final exam3 hrs		
TOTAL 175 hrs to match 25 x 7 ECTS		
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