COURSE PROFILE

| Course Name | Code | Semester | Term | Theory <br> +PS+Lab. <br> (hour/week) | Local Credits |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Mathematical Theory of Fluids | MATH <br> 451 | Fall | 7 | $3+0+0$ | 3 |


| Prerequisites | None |
| :--- | :--- |


| Course Language | English |
| :---: | :---: |
| Course Type | Elective |
| Course Lecturer | - Prof.Dr. Hilmi Demiray |
| Course Assistant | -- |
| Course Objectives | The aim of this course is to present a mathematical model for fluids and then solve these model equations under the effect of external agencies. |
| Course Learning Outcomes | The students who succeeded in this course; <br> - will be able to characterize the behaviour of a fluid body by a mathematical expression (mathematical modelling). <br> - will be able to understand the physical characterization of various differential equations. <br> - will be able to characterize some phenomenon existing in the nature by some mathematical formulas and interpret the resulting solution. <br> - will be able to understand the origin of some phenomenon like sound and its propagation as a wave. |
| Course Content | Mathematical preliminaries, definitions, kinematics of fluids. Material derivative, velocity and acceleration vectors. Path and flow lines, vortex, equations of motion, stress. Constitutive equations, hydrostatics. Ideal fluids, Bernoulli theorems, incompressible ideal fluids. Potential flows, vortex flows, surface waves, viscous flids, Stokes approximations, boundary layer theory. |

## COURSE CONTENT

| Week | Subjects | Related Preparation |
| :--- | :--- | :--- |
| 1 | Definitions and classification of fluids, mathematical preliminaries, vectors and <br> tensors, gradient of scalars and vectors. | Chapter 1,2 |


| 2 | Curvilinear coordinates, cylindrical and spherical coordinates, integral theorems, Green- Gauss theorems, Stokes theorems. | Chapter 2 |
| :---: | :---: | :---: |
| 3 | Kinematics of fluids: motion, material derivative, and acceleration vectors, path and flow lines, velocity field around a point: deformation rate and vorticity tensors. | Chapter 3 |
| 4 | Transport theorems, jump conditions, Balance laws: conservation of mass, balance of linear and angular momenta, balance of energy, stress at a point, stress tensor. | Chapter 4 |
| 5 | Moving coordinate systems, circulation, constitutive equations, Helmholtz resolution theorem, ideal fluids, viscous fluids, equations of ideal fluids in various coordinate systems. | Chapter 4 |
| 6 | Bernoulli's theorems, incompressible ideal fluids, flows in two dimension, axially symmetric flows. | Chapter 4, 6 |
| 7 | Potential flows. Midterm I. | Chapter 6 |
| 8 | Potential flow (continued), sphere in a uniform flow. | Chapter 6 |
| 9 | Sphere in rectilinear motion, plane potential flows. | Chapter 6 |
| 10 | Uniform plane flows, source and sink problems. | Chapter 6 |
| 11 | The use of complex functions in solving plane flow problems. | Chapter 6 |
| 12 | Blausius theorems, Blausius theorems for a cylinder in motion, theorem for a circular disc. | Chapter 6 |
| 13 | Blausius theorems and applications (continued). Midterm II. | Chapter 6 |
| 14 | Conform mapping and its applications to plane flow. | Chapter 6 |


| Course Textbooks | Fluid Mechanics, 3rd Edition, Pijush K. Kunda and Ira M. Cohen, Elsevier Academic Press, <br> 2004. |
| :--- | :--- |
| Recommended <br> References | Any book on fluid dynamics. |


| Attendance/Participation | - | - |
| :---: | :---: | :---: |
| Laboratory | - | - |
| Application | - | - |
| Special Course Internship (Work Placement) | - | - |
| Quizzes/Studio Critics | - | - |
| Homework Assignments | 7 | 10 |
| Presentation | - | - |
| Project | - | - |
| Seminar/Workshop | - | - |
| Midterms/Oral Exams | 1 | 40 |
| Final/Resit Exam | 1 | 50 |
| Total | 9 | 100 |


| PERCENTAGE OF SEMESTER WORK | 8 | 50 |
| :--- | :--- | :--- |
| PERCENTAGE OF FINAL WORK | 1 | 50 |
| Total | 9 | 100 |


| Course Category | Core Courses | X |
| :--- | :--- | :--- |
|  | Major Area Courses |  |
|  | Supportive Courses |  |
|  | Media and Management Skills Courses |  |
|  | Transferable Skill Courses |  |

## COURSE'S CONTRIBUTION TO PROGRAM

| \# | Program Qualifications / Outcomes | * Level of Contribution |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 1 | 2 | 3 | 4 | 5 |
| 1 | To have a grasp of basic mathematics, applied mathematics and theories and applications of statistics. |  |  |  |  | X |
| 2 | To be able to use theoretical and applied knowledge acquired in the advanced fields of mathematics and statistics, |  |  |  |  | X |


| 3 | To be able to define and analyze problems and to find solutions based on scientific methods, |  |  |  |  | X |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | To be able to apply mathematics and statistics in real life with interdisciplinary approach and to discover their potentials, |  |  |  |  | X |
| 5 | To be able to acquire necessary information and to make modeling in any field that mathematics is used and to improve herself/himself, |  |  |  |  | X |
| 6 | To be able to criticize and renew her/his own models and solutions, |  |  |  |  | X |
| 7 | To be able to tell theoretical and technical information easily to both experts in detail and nonexperts in basic and comprehensible way, |  |  | X |  |  |
| 8 | To be able to use international resources in English and in a second foreign language from the European Language Portfolio (at the level of B1) effectively and to keep knowledge up-to-date, to communicate comfortably with colleagues from Turkey and other countries, to follow periodic literature, |  |  |  | X |  |
| 9 | To be familiar with computer programs used in the fields of mathematics and statistics and to be able to use at least one of them effectively at the European Computer Driving Licence Advanced Level, |  |  | X |  |  |
| 10 | To be able to behave in accordance with social, scientific and ethical values in each step of the projects involved and to be able to introduce and apply projects in terms of civic engagement, |  |  | X |  |  |
| 11 | To be able to evaluate all processes effectively and to have enough awareness about quality management by being conscious and having intellectual background in the universal sense, |  |  | X |  |  |
| 12 | By having a way of abstract thinking, to be able to connect concrete events and to transfer solutions, to be able to design experiments, collect data, and analyze results by scientific methods and to interfere, |  |  |  | X |  |
| 13 | To be able to continue lifelong learning by renewing the knowledge, the abilities and the compentencies which have been developed during the program, and being conscious about lifelong learning, |  |  |  |  |  |
| 14 | To be able to adapt and transfer the knowledge gained in the areas of mathematics and statistics to the level of secondary school, |  |  | X |  |  |
| 15 | To be able to conduct a research either as an individual or as a team member, and to be effective in each related step of the project, to take role in the decision process, to plan and manage the project by using time effectively. |  |  |  |  |  |

[^0]ECTS ALLOCATED BASED ON STUDENT WORKLOAD BY THE COURSE DESCRIPTION

| Activities | Number | Duration (Hours) | Total Workload |
| :---: | :---: | :---: | :---: |
| Course Hours (Including Exams) | 14 | 3 | 48 |
| Tutorials | - | - | - |
| Laboratory | - | - | - |
| Application | - | - | - |
| Special Course Internship (Work Placement) | - | - | - |
| Field Work | - | - | - |
| Study Hours Out of Class | 14 | 2 | 28 |
| Presentations / Seminar | - | - | - |
| Project | - | - | - |
| Preparatory reading | 13 | 2 | 26 |
| Homework Assignments | 7 | 3 | 21 |
| Quizzes | - | - | - |
| Midterm Exams | 1 | 9 | 9 |
| Final / Resit Exam | 1 | 18 | 18 |
|  |  | Total Workload | 150 |

COURSE CATEGORY
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\begin{array}{|l|l|l|l|l|}\hline \begin{array}{l}\text { ISCED } \\
\text { GENERAL } \\
\text { AREA } \\
\text { CODES }\end{array}
$$ \& GENERAL AREAS \& ISCED <br>
BASiC AREA <br>

CODES\end{array}\right)\) BASIC EDUCATIONAL AREAS |  |
| :--- |
| 1 |


| 3 | Social Sciences, Management and Law | 38 | Law | 0 |
| :---: | :---: | :---: | :---: | :---: |
| 4 | Science | 42 | Life Sciences | 0 |
| 4 | Science | 44 | Natural Sciences | 0 |
| 4 | Science | 46 | Mathematics and Statistics | 70 |
| 4 | Science | 48 | Computer | 0 |
| 5 | Engineering, Manufacturing and Civil | 52 | Engineering | 30 |
| 5 | Engineering, Manufacturing and Civil | 54 | Manufacturing and Processing | 0 |
| 5 | Engineering, Manufacturing and Civil | 58 | Architecture and Structure | 0 |
| 6 | Agriculture | 62 | Agriculture, Forestry, Livestock, Fishery | 0 |
| 6 | Agriculture | 64 | Veterinary | 0 |
| 7 | Medicine and Welfare | 72 | Medical | 0 |
| 7 | Medicine and Welfare | 76 | Social Services | 0 |
| 8 | Service | 81 | Personal Services | 0 |
| 8 | Service | 84 | Transport Services | 0 |
| 8 | Service | 85 | Environment Protection | 0 |
| 8 | Service | 86 | Security Services | 0 |


[^0]:    *1 Lowest, 2 Low, 3 Average, 4 High, 5 Highest

